## 582. Molecular Polarisability. The Conformations of Certain Amides as Solutes in Dioxan

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Dipole moments and molar Kerr constants are reported for formamide ( 3.85 D and $284 \times 10^{-12}$ ), $N$-methylformamide $\left(3.84 \mathrm{p}\right.$ ) and $210 \times 10^{-12}$ ), $N N$-dimethylformamide $\left(3.91 \mathrm{D}\right.$ and $\left.417 \times 10^{-12}\right)$, $N$-t-butylformamide ( 3.94 D and $336 \times 10^{-12}$ ), $N N$-diphenylformamide ( 3.44 D and $406 \times 10^{-12}$ ), acetamide ( 3.87 D and $257 \times 10^{-12}$ ), $N$-t-butylacetamide ( 3.85 D and $195 \times$ $10^{-12}$ ), and benzamide ( $3 \cdot 76 \mathrm{n}$ and $234 \times 10^{-12}$ ) as solutes in dioxan at $25^{\circ}$. The data are analysed to indicate that (a) the trans-isomer abundances for $N$-methylformamide and $N$-t-butylformamide are 90 and $c a .71 \%$, respectively, (b) benzamide in dioxan is non-planar, the dihedral angle between the benzene ring and the plane of the amide group being $37^{\circ} \pm 5^{\circ}$, and (c) the preferred conformation of $N N$-diphenylformamide is attained by rotations (in the same sense) of both phenyl groups through $52^{\circ} \pm 5^{\circ}$ from a theoretical planar model.

This Paper is concerned with the experimental determination of the dipole moments and molar Kerr constants of a number of acid amides, and with the analysis of such data to yield information on the configurations of these molecules as solutes at high dilution in dioxan.

Table 1
Incremental Kerr constants, dielectic constants, densities, and refractive indices for solutions in dioxan at $25^{\circ}$

| Formamide |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{5} w_{2} \quad \ldots$ | 515 | 583 | 753 | 850 | 1081 | 1258 | 1570 | 2083 |
| $10^{7} \Delta B \ldots$ | $0 \cdot 180$ | $0 \cdot 203$ | $0 \cdot 264$ | $0 \cdot 306$ | $0 \cdot 410$ | 0.515 | $0 \cdot 629$ | 0.818 |
| $\varepsilon^{25} \ldots \ldots \ldots$ | $2 \cdot 4195$ | $2 \cdot 4480$ | $2 \cdot 5144$ | - | $2 \cdot 6466$ |  | $2 \cdot 8471$ | $3 \cdot 0701$ |
| whence $\Sigma 10^{7} \Delta B / \Sigma w_{2}=38.2 ; ~ \Sigma \Delta \varepsilon / \Sigma w_{2}=40.9$ |  |  |  |  |  |  |  |  |
| $10^{5} w_{2} \quad \ldots$ | 1215 | 1386 | 1510 | 2184 | 2829 | 3853 |  |  |
| $10^{4} \Delta n$.. |  | 4 |  | 6 | 8 | 11 |  |  |
| $d_{4}{ }^{25} \ldots \ldots$ | 1.02961 | 1.02984 | 1.03000 | 1.03093 | 1.03174 | 1.03310 |  |  |
| whence $\Sigma \Delta n / \Sigma w_{2}=0.028 ; ~ \Sigma \Delta d / \Sigma w_{2}=0.133$ |  |  |  |  |  |  |  |  |
| N-Methylformamide |  |  |  |  |  |  |  |  |
| $10^{5} \omega_{2} \quad \ldots$ | 342 | 430 | 515 | 545 | 618 | 771 | 849 | 974 |
| $10^{7} \Delta B \ldots$ | $0 \cdot 088$ | $0 \cdot 106$ | $0 \cdot 129$ | $0 \cdot 146$ | $0 \cdot 170$ | 0.221 | $0 \cdot 262$ | $0 \cdot 289$ |
| whence $10^{7} \Delta B=21 \cdot 8 w_{2}+889 w_{2}{ }^{2}$ |  |  |  |  |  |  |  |  |
| $10^{5} w_{2} \quad \ldots$ | 375 | 505 | 567 | 824 | 1074 | 1292 | 1769 | 2075 |
| $\varepsilon^{25} \ldots \ldots \ldots$ | $2 \cdot 3238$ | $2 \cdot 3818$ | $2 \cdot 3903$ | $2 \cdot 4820$ | 2.5745 | 2.6851 | $2 \cdot 8610$ | 2.9920 |
| whence $\Delta \varepsilon=30 \cdot 95{ }_{5} w^{\prime}+333 w_{2}{ }^{2}$ |  |  |  |  |  |  |  |  |
| $10^{5} 2 e_{2} \ldots$ | 1137 | 1554 | 2109 | 3232 | 6691 |  |  |  |
| $10^{4} \Delta n \ldots$ | - | - | 2 | 3 | 7 |  |  |  |
| $d_{4}{ }^{25} \ldots \ldots$. | 1.02793 | 1.02791 | 1.02788 | 1.02777 | 1.02753 |  |  |  |
| whence $\Sigma \Delta n / \Sigma \chi_{2}=0.010 ; ~ \Sigma \Delta d / \Sigma w_{2}=-0.006_{7}$ |  |  |  |  |  |  |  |  |


| $10^{5} w_{2}$ | $\ldots$ | 472 | 485 | 704 | 780 | 1035 | 1287 | 1751 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{7} \Delta B$ | 0 | $0 \cdot 149$ | - | $0 \cdot 248$ | $0 \cdot 253$ | $0 \cdot 347$ | $0 \cdot 428$ | 0.638 |
| $\varepsilon^{25} \ldots \ldots \ldots$ | - | $2 \cdot 3351$ | - | $2 \cdot 4114$ | $2 \cdot 4751$ | $2 \cdot 5426$ | $2 \cdot 6645$ |  |

whence $\Sigma 10^{7} \Delta B / \Sigma w_{2}=34 \cdot 2 ; \Sigma \Delta \varepsilon / \Sigma w_{2}=25 \cdot 9$

| $10^{5} w_{2}$ | $\cdots$ | 980 | 1572 | 1947 | 2606 | 3527 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $d_{25}$ |  | .02704 | 1.02649 | 1.02611 | 1.02552 | 1.02459 |

$d_{4}{ }^{25} \ldots . .1 .02704 \quad 1.02649 \quad 1.02611 \quad 1.02552 \quad 1.02459$
whence $\Sigma \Delta d / \Sigma w_{2}=-0.096 ; \Delta n=c a .0$ for concentrations up to $w_{2}=0.03$

| N-t-Butylformamide |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{array}{ll} 10^{6} w_{2} & \ldots \\ 10^{7} \Delta B & \ldots \end{array}$ | 2543 | 3551 | 4404 | 5510 | $10^{5} w_{2}$ | 2700 | 5908 | 10,885 |
|  | $0 \cdot 0527$ | $0 \cdot 0672$ | $0 \cdot 0919$ | $0 \cdot 1076$ | $10^{4} \Delta n$ | 3 |  | 13 |
|  | whence $\Sigma 10^{7} \Delta B / \Sigma w_{2}=20.0$ |  |  |  |  | whence $\Sigma \Delta n / \Sigma w_{2}=0.011$ |  |  |
| $10^{5} w_{2} \ldots$ | 519 | 698 | 976 | 1175 | 1279 | 1720 | 2138 | 2215 |
| $\varepsilon^{25}$.. | 2.3074 | $2 \cdot 3411$ | $2 \cdot 3952$ | 2.4315 | $2 \cdot 4568$ | $2 \cdot 5345$ | $2 \cdot 6160$ | $2 \cdot 6352$ |
| $d_{4}{ }^{25}$ | 1.02726 | 1.02706 | 1.02666 | - | 1.02615 | 1.02560 | - | 1.02491 |

whence $\Sigma \Delta \varepsilon_{1} / \Sigma \psi_{2}=19 \cdot 1 ; \Sigma \Delta d / \Sigma w_{2}=-0 \cdot 140$

| $\begin{aligned} & 10^{5} w_{2} \\ & 10^{7} \Delta B \end{aligned}$ | NN-Diphenylformamide |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 204 | 375 | 508 | 594 | 697 |  |
|  | 0.0252 | 0.0468 | 0.0623 | $0 \cdot 0700$ | $0 \cdot 0870$ |  |
|  | whence $\Sigma 10^{7} \Delta B / \Sigma w_{2}=12 \cdot 3$ |  |  |  |  |  |
| $10^{5} w_{2}$ | 339 | 609 | 910 | 1315 | 1733 | 2679 |
| $10^{4} \Delta n$ |  | 10 | - | 21 | 29 | 44 |
| $\varepsilon^{25}$ | $2 \cdot 2263$ | $2 \cdot 2565$ | 2.2803 | 2.3122 | $2 \cdot 3454$ | $2 \cdot 4209$ |
| $d_{4}{ }^{25}$ | $1 \cdot 02840$ | - | $1 \cdot 02906$ | 1.02954 | 1.02995 | 1.03098 |


| Acetamide |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{5} w_{2} \quad \ldots$ | 431 | 523 | 644 | 733 | 851 | 1619 | 2060 |
| $10^{7} \Delta B \ldots$ | $0 \cdot 108$ | $0 \cdot 127$ | 0.172 | $0 \cdot 182$ | $0 \cdot 240$ | 0.417 | 0.566 |
| whence $\Sigma 10^{7} \Delta B / \Sigma w_{2}=26.4$ |  |  |  |  |  |  |  |
| $10^{5} \mu_{2} \quad \ldots$ | 1250 | 1715 | 1973 | 2352 | 2766 |  |  |
| $10^{4} \Delta n \ldots$ | 1 | 1 | 2 | 2 | 2 |  |  |
| $d_{4}{ }^{25} \ldots \ldots$. | 1.02844 | $1 \cdot 02859$ | 1.02870 | $1 \cdot 02880$ | 1.02891 |  |  |
| whence $\Sigma \Delta n / \Sigma w_{2}=0.008 ; \Sigma \Delta d / \Sigma w_{2}=0.034$ |  |  |  |  |  |  |  |
| $10^{5} w_{2}$. | 532 | 801 | 1124 | 1616 | 2014 |  |  |
| $\varepsilon^{25} \ldots \ldots \ldots$. | $2 \cdot 3752$ | 2.4583 | 2.5582 | 2.7164 | $2 \cdot 8466$ |  |  |



## Experimental

Materials, Apparatus, etc.- $N$-t-Butylformamide, prepared by the addition of a solution of sulphuric acid in acetic acid to a mixture ${ }^{1}$ of $t$-butyl alcohol, sodium cyanide, and acetic acid, had b. p. $200-202^{\circ}$. $N$-t-Butylacetamide, prepared by passing gaseous isobutene (generated from a heated t-butyl alcohol-conc. sulphuric acid mixture) into a solution ${ }^{2}$ of acetonitrile, acetic acid, and sulphuric acid, had m. p. $98^{\circ}$ (from hexane). The other solutes were commercial samples which on purification gave: formamide, b. p. $79^{\circ} / 6 \mathrm{~mm}$.; $N$-methylformamide, b. p. $82^{\circ} / 10 \mathrm{~mm} . ; N N$-dimethylformamide, b. p. $76^{\circ} / 39 \mathrm{~mm} . ; N N$-diphenylformamide, m. p. $73.5^{\circ}$; acetamide, m. p. $80^{\circ}$; benzamide, m. p. $128^{\circ}$.

Apparatus, techniques, symbols used, and methods of calculation have been described before. ${ }^{3-5}$ Observations are recorded in Table 1 and results summarised in Table 2. The quantities $\Delta \varepsilon, \Delta d, \Delta n$, and $\Delta B$ are the differences found between the dielectric constants, densities, refractive indices, and Kerr constants, respectively, of the solvent and of solutions containing weight fractions $w_{2}$ of solute. The following data apply at $25^{\circ}$ to dioxan: $\varepsilon_{1}=$ $2.2090 ; \quad d_{1}=1.0280 ; \quad\left(n_{\mathrm{D}}\right)_{1}=1.4202 ; \quad 10^{7} B_{1}=0.068 ; \quad 10_{\mathrm{s}}^{12} K_{1}=0.0116$.

## TAble 2

Dielectric polarisations, dipole moments, and molar Kerr constants (from observations on solutions in dioxan at $25^{\circ}$ )

| Solute | $\alpha \varepsilon_{1}$ | $\beta$ | $\gamma$ | $\delta$ | $\infty_{\infty} P_{2}$ (c.c.) | $R_{\mathrm{D}}$ (c.c.) | $\mu(\mathrm{D})$ * | $10^{12}{ }_{\infty}\left({ }_{m} K_{2}\right) \ddagger$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Formamide | 40.9 | $0 \cdot 129$ | 0.02 | 562 | 314 | $10 \cdot 3$ | 3.85 | 284 |
| $N$-Methylformamide | $30 \cdot 9$ ¢ $\dagger$ | $-0.007$ | 0.01 | $321 \dagger$ | 317 | 14.9 | $3 \cdot 84$ | 210 |
| $N N$-Dimethylformamide | $25 \cdot 9$ | -0.094 | 0 | 503 | 334 | $19 \cdot 7$ | 3.91 | 417 |
| N-t-Butylformamide..... | $19 \cdot 1$ | $-0.136$ | 0.01 | 294 | 350 | 28.9 | 3.94 | 336 |
| $N N$-Diphenylformamide | 7.88 | $0 \cdot 111$ | $0 \cdot 12$ | 180 | 305 | $59 \cdot 8$ | 3.44 | 406 |
| Acetamide ..... | $31 \cdot 4$ | 0.033 | 0.01 | 388 | 321 | 14.3 | 3.87 | 257 |
| N -t-Butylacetamide | $15 \cdot 9 \dagger$ | $-0.145$ | 0.01 | $153 \dagger$ | 337 | $33 \cdot 2$ | $3 \cdot 85$ | 195 |
| Benzamide | $14 \cdot 9$ | $0 \cdot 143$ | $0 \cdot 11$ | 173 | 326 | $34 \cdot 9$ | $3 \cdot 76$ | 234 |

* Calculated assuming ${ }_{\mathrm{D}} P=1.05 R_{\mathrm{D}}$; uncertainty in $\mu c a . \pm 0.03 \mathrm{D}$. $\dagger$ Variation of $\varepsilon_{12}$ or $B_{12}$ with $w_{2}$ was non-linear over the concentration range studied; the experimental data ( $\Delta \varepsilon$ or $\Delta B$ ) were fitted to a regression equation of the form $\Delta \varepsilon=a w_{2}+b w_{2}{ }^{2}$, and subsequent extrapolation to $w_{2}=0$ resulted in the coefficients $\alpha \varepsilon_{1}$ or $\delta$ here recorded. $\ddagger$ Uncertainty in $\infty\left({ }_{m} K_{2}\right)$ values is estimated at $\pm 5 \%$.

Previous Measurements.-McClellan ${ }^{6}$ lists the following values for dipole moments (D) in dioxan: formamide, $3 \cdot 0,{ }^{7} 3 \cdot 86 ;^{8}$ acetamide, $3 \cdot 90,{ }^{8} 3 \cdot 6,{ }^{9} 3 \cdot 92 ;{ }^{10}$ benzamide, $3 \cdot 84,{ }^{8} 3 \cdot 6,{ }^{9} 3 \cdot 80,{ }^{11}$ $3.88 .{ }^{12}$ In addition, the following values (in dioxan) were recorded by Lee and Kumler: ${ }^{13}$ $N N$-dimethylformamide, $3 \cdot 95$; acetamide, $3 \cdot 70$. The vapour phase dipole moments, recently reported ${ }^{14}$ for $N$-methylformamide (3.82), $N N$-dimethylformamide (3.80), and acetamide $(3 \cdot 75)$, are similar to the values (in Table 2) now derived by extrapolation to infinite dilution in dioxan.

## Discussion

Bond and Group Polarisabilities.-Initially we examine the degree of applicability of bond polarisability data previously recorded ${ }^{15}\left[b_{\mathrm{L}}(\mathrm{H}-\mathrm{N})=0.50, b_{T}(\mathrm{H}-\mathrm{N})=b_{V}(\mathrm{H}-\mathrm{N})=\right.$
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$0.83 ; \quad b_{\mathrm{L}}(\mathrm{C}-\mathrm{N})=0.57, \quad b_{\mathrm{T}}(\mathrm{C}-\mathrm{N})=b_{\mathrm{V}}(\mathrm{C}-\mathrm{N})=0.69 ; \quad b_{\mathrm{L}}(\mathrm{C}=\mathrm{O})=2.30, \quad b_{\mathrm{T}}(\mathrm{C}=\mathrm{O})=1.40$, $\left.b_{\mathrm{V}}(\mathrm{C}=\mathrm{O})=0.46 ; \quad b_{\mathrm{L}}(\mathrm{C}-\mathrm{H})=b_{\mathrm{T}}(\mathrm{C}-\mathrm{H})=b_{\mathrm{V}}(\mathrm{C}-\mathrm{H})=0.64\right] *$ to the calculation of molecular parameters for the amides. For a planar model (I) of formamide, ${ }^{16}$ the polarisability tensor is specified, by addition ${ }^{5}$ of the component bond ellipsoids, as: $b_{1}$ (calc.) $=4 \cdot 87$, $b_{2}$ (calc.) $=4.04, b_{3}$ (calc.) $=3.45$, where $b_{1}$ and $b_{2}$ are located in the plane of symmetry such that the $b_{1}$ axis makes an angle of $50^{\circ}$ with $\mathrm{N}-\mathrm{C}$ and $10^{\circ}$ with $\mathrm{C}=0$. If the permanent electric moment $(3.85 \mathrm{D})$ acts at $40^{\circ}$ to the $\mathrm{N}-\mathrm{C}$ bond (found from Stark effect measure-

(I)

(II) trans

(III) cis
ments by Kurland and Bright Wilson ${ }^{16}$ ), then the vector components along the principal axes are: $\mu_{1}=3.79 \mathrm{D}, \mu_{2}=0.67 \mathrm{D}$, and $\mu_{3}=0$. Substitution of these values in equations (1)-(3) leads to a predicted molar Kerr constant of $178 \times 10^{-12}$ (assuming ${ }_{\mathrm{D}} P /{ }_{\mathrm{k}} P=1 \cdot 1$ ) which is considerably lower than that observed $\left(284 \times 10^{-12}\right)$. Clearly the $\mathrm{H}-\mathrm{N}, \mathrm{C}-\mathrm{N}$, and $\mathrm{C}=\mathrm{O}$ bond polarisabilities listed above, which were derived from simple molecules, cannot be used to specify the highly resonating amide group $\left[>\mathrm{N}-\mathrm{C}=\mathrm{O}>\stackrel{+}{\mathrm{N}}=\mathrm{C}^{+}-\mathrm{O}^{-}\right]$.

$$
\begin{align*}
{ }_{\mathrm{m}} K & =2 \pi \boldsymbol{N}\left(\theta_{1}+\theta_{2}\right) / 9  \tag{1}\\
\theta_{1} & ={ }_{\mathrm{p}} P\left[\left(b_{1}-b_{2}\right)^{2}+\left(b_{2}-b_{3}\right)^{2}+\left(b_{3}-b_{1}\right)^{2}\right] / 45 \boldsymbol{k} T_{\mathrm{F}} P  \tag{2}\\
\theta_{2} & =\left[\left(b_{1}-b_{2}\right)\left(\mu_{1}^{2}-\mu_{2}^{2}\right)+\left(b_{2}-b_{3}\right)\left(\mu_{2}^{2}-\mu_{3}^{2}\right)+\left(b_{3}-b_{1}\right)\left(\mu_{3}^{2}-\mu_{1}^{2}\right)\right] / \mathbf{4} \boldsymbol{5} \boldsymbol{k}^{2} T^{2} \tag{3}
\end{align*}
$$

The quantity $\left(\theta_{1}+\theta_{2}\right)$ is calculable for formamide from the observed molar Kerr constant [using equation (1)] as $67.5 \times 10^{-35}$. Since $\mu\left(o b s\right.$.) is large, then $\theta_{1} \leqslant \theta_{2}$, and as $\left(\theta_{1}+\theta_{2}\right)$, and hence $\theta_{2}$, are very great and positive, it follows that the maximum polarisability axis must be located very near to the dipole-moment direction. If we make the reasonable approximations that $\theta_{1}=0$ and $\mu_{1}=\mu$ (obs.), equations (1), (3), and (4) can be solved, to yield values of $b_{1}(=5 \cdot 04)$ and $\left(b_{2}+b_{3}\right)(=6.60)$.

$$
\begin{equation*}
\mathrm{E}^{P}=0.95 R_{\mathrm{D}}=4 \pi \mathbf{N}\left(b_{1}+b_{2}+b_{3}\right) / 9 \tag{4}
\end{equation*}
$$

Similar considerations can safely be applied to each of the aliphatic amides of Table 2. The estimates of $b_{1}$ and of $\left(b_{2}+b_{3}\right)$ thus obtained are listed in Table 3. Further, the observed moments for these molecules are virtually constant (all lie within the range $3.89 \pm 0.05 \mathrm{D}$ ), so we will assume that, in each case, $\mu$ (obs.), and hence $b_{1}$, are located as shown in (I) for formamide.

Table 3
Polarisability semi-axes


La Planche and Rogers ${ }^{17}$ recently showed from an n.m.r. spectral study of $N$-monosubstituted amides, that N -t-butylacetamide, unlike the corresponding formamide, exists exclusively as the trans-configuration (II). We accept this in the following discussion. If, then, the $\mathrm{C}-\mathrm{C}$ and $\mathrm{C}-\mathrm{H}$ link polarisability contributions ${ }^{\mathbf{1 5}}\left[b_{\mathrm{L}}(\mathrm{C}-\mathrm{C})=0.99, b_{\mathrm{T}}(\mathrm{C}-\mathrm{C})=\right.$ $\left.b_{V}(\mathrm{C}-\mathrm{C})=0.27\right]$ of the t-butyl group are subtracted from $b_{1}(N$-t-butylacetamide) we are

[^0]left with $b_{1}\left[\mathrm{C}(\right.$ trans $\left.) \cdot \mathrm{NH} \cdot \mathrm{CO} \cdot \mathrm{CH}_{3}\right]=5 \cdot 81$. Comparison of this quantity with $b_{1}$ (acetamide) shows that substitution of an $\mathrm{N}-\mathrm{H}$ by an $\mathrm{N}-\mathrm{C}$ link wholly in the trans-position results in an incremental change in $b_{1}$ of -0.61 . A similar substitution in the cis-position leads to a change in $b_{1}$ of +0.79 [from $b_{1}\left(N N\right.$-dimethylformamide), $b_{1}$ (formamide), and $\Delta b_{1}(\operatorname{trans})=$ $-0.61]$. It is possible, on this basis, to predict, from $b_{1}$ (formamide), the theoretical values of $b_{1}($ trans $)$ and $b_{1}(c i s)$ for $N$-methylformamide and for $N$-t-butylformamide. The calculations are summarised in Table 4. It should be noted that in all cases considered the amide group is assumed to be planar. We thus conclude that, in dioxan solution, each of these molecules exist in both the cis- and trans-configurations, with the latter predominant. The trans-isomer abundances recorded in Table 4 agree reasonably with those ( $92 \%$ for N -methylformamide and $\mathbf{8 2} \%$ for N -t-butylformamide) given by La Planche and Rogers. ${ }^{17}$

Table 4

| Compound |  |  | $b_{1}($ trans $)$ | $+b_{3}($ trans $\left.)\right]$ | ${ }_{\mathrm{m}} K($ trans $)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (i) | N-Methylfor | mide | 6.35 | 10.54 | $176 \times 10^{-12}$ |
| (ii) | N -t-Butylf | mide .............. | 11.93 | $20 \cdot 65$ | 275 |
| (i) | $b_{1}(c i s)$ | $\left[b_{2}(c i s)+b_{3}(c i s)\right]$ | ${ }_{\mathrm{m}} K(c i s)$ | ${ }_{\mathrm{m}} K$ (obs.) | \% trans |
|  | 7.75 | $9 \cdot 14$ | $518 \times 10^{-12}$ | $210 \times 10^{-12}$ | 90 |
| (ii) | 12.74 | 19.84 | 483 | 336 | $c a .71 *$ |

* $b_{1}($ trans $)$ and $b_{1}(c i s)$ are not sufficiently divergent to allow a precise estimate of the trans: cis ratio.

Benzamide.-Specification of the molecular polarisability tensor can be effected by additivity of the component $\mathrm{C}_{6} \mathrm{H}_{5}$ and $\mathrm{H}_{2} \mathrm{~N} \cdot \mathrm{CO} \cdot \mathrm{C}$ group semi-axes. In the calculations, the following data were used [for $\mathrm{C}_{6} \mathrm{H}_{5}$ (ref. 15) and $\mathrm{H}_{2} \mathrm{~N} \cdot \mathrm{CO} \cdot \mathrm{C}$,* respectively]: $b_{1}, 10.56$ and $4.50 ; b_{2}, 10.56$ and $2.95 ; b_{3}, 6.72$ and 2.95 .

Table 5
Polarisabilities and molar Kerr constants calculated for conformations of benzamide

| $\phi \quad b_{1}$ (calc.) |  |  |  | $10^{12}{ }_{\mathrm{m}} K$ (calc.) |
| :---: | :---: | :---: | :---: | :---: |
|  | $X$ | $Y$ | $Z$ |  |
| - $\left\{\begin{array}{l}b_{1}=15.06\end{array}\right.$ | +0.771 | $+0.637$ | 0 |  |
| $0^{\circ}\left\{b_{2}=13.51\right.$ | $+0.637$ | $-0.771$ | 0 | $+554$ |
| $\left\{b_{3}=9.67\right.$ | 0 | 0 | $+1$ |  |
| $\left\{b_{1}=13.51\right.$ | $+0.627$ | $-0.775$ | $+0.076$ |  |
| $26^{\circ}\left\{b_{2}=14.85\right.$ | $+0.721$ | $+0.615$ | $+0.318$ | +383 |
| $b_{3}=9.89$ | $-0.293$ | $-0.144$ | $+0.945$ |  |
| $b_{1}=13.51$ | $+0.626$ | $-0.772$ | $+0.113$ |  |
| $36^{\circ}\left\{b_{2}=14.66\right.$ | $+0.666$ | $+0.604$ | $+0.438$ | $+247$ |
| $b_{3}=10.07$ | $-0.407$ | $-0.199$ | $+0.892$ |  |
| $\left\{b_{1}=11 \cdot 16\right.$ | - 0.0 .912 | +0.411 | 0 |  |
| $90^{\circ}\left\{b_{2}=13.57\right.$ | $-0.411$ | $+0.912$ | 0 | -335 |
| $b_{3}=13.51$ | 0 | 0 | $+1$ |  |

Table 5 lists the polarisability semi-axes and molar Kerr constants calculated for conformations of benzamide defined by angles $\phi$ (where $\phi$ is the dihedral angle between the planes of the amide group and of the aromatic ring; e.g., for a planar molecule, $\phi=0^{\circ}$ ). The permanent electric moment components in the $X, Y$, and $Z$ directions (see Figure 1) are: $\mu_{x}=3.76 \cos 40 ; \mu_{y}=3.76 \sin 40 ; \mu_{z}=0$. The observed molar Kerr constant $\left(+234 \times 10^{-12}\right)$ is lower than that calculated for the solid-state configuration ( $\phi=26^{\circ}$ from an $X$-ray analysis by Penfold and White ${ }^{18}$ ) and corresponds to an angle $\phi$ of $c a .37^{\circ}$. The uncertainty in $\phi$, though difficult to assess, may reasonably be taken as $\pm 5^{\circ}$.

[^1]NN-Diphenylformamide.-Polarisability parameters and molar Kerr constants computed for conformations of $N N$-diphenylformamide are given in Table 6. The polarisabilities of the $\mathrm{C}_{2} \mathrm{~N} \cdot \mathrm{CO} \cdot \mathrm{H}$ group were taken as $b_{1}=5 \cdot 22, b_{2}=b_{3}=\mathbf{2 \cdot 7 6}$, i.e., the semi-axes of $N N$-dimethylformamide (assuming axial symmetry) less six $\mathrm{C}-\mathrm{H}$ link contributions. The electric moment components along the reference axes $X, Y, Z$, were calculated on the


Figure 1


Figure 2
basis that $\mu$ ( $N N$-diphenylformamide) is resolvable into $\mu_{\mathrm{a}}$ and $\mu_{\mathrm{b}}$, where $\mu_{\mathrm{a}}$ is equivalent to the moment of $N N$-dimethylformamide and $\mu_{\mathrm{b}}$ is the vector sum of mesomeric moments directed along each $\mathrm{N}^{+\rightarrow} \mathrm{C}_{\text {ar }}$ axis. From $\mu($ resultant $)=3.44 \mathrm{D}$ and $\mu_{a}=3.91 \mathrm{D}$, the magnitude of $\mu_{\mathrm{b}}$ follows as $0.6_{5}$ D and the location of $\mu$ (resultant) as $47^{\circ}$ from the $X$ direction (see Figure 2). The calculated molecular refraction obtained ${ }^{19}$ as $R(N N$-dimethylform-

Table 6
Polarisabilities and molar Kerr constants calculated for conformations of NN -diphenylformamide

| $\alpha \quad b_{1}$ (calc.) | $X$ | $Y$ | $\bar{Z}$ | $10^{12}{ }_{\mathrm{m}} \mathrm{K}$ (calc.) |
| :---: | :---: | :---: | :---: | :---: |
| , $b_{1}=24.54$ | $+0.723$ | $-0.691$ | 0 |  |
| $0^{\circ}\left\{b_{2}=26.93\right.$ | $+0.691$ | $+0.723$ | 0 | 904 |
| $b_{3}=16.20$ | 0 | 0 | $+1$ |  |
| 「 $b_{1}=21.88$ | $+0.922$ | $-0.170$ | $-0.348$ |  |
|  |  |  | (+) |  |
| $52^{\circ}\left\{b_{2}=25.72\right.$ | +0.295 | $+0.889$ | $\underset{(-)}{+0.349}$ | 409 * |
| $b_{3}=20.06$ | $\underset{(-)}{+0 \cdot 251}$ | $\frac{-0.424}{(+)}$ | +0.870 |  |
| $\left\{b_{1}=19 \cdot 60\right.$ | $+0.965$ | $-0.264$ | 0 |  |
| $90^{\circ}\left\{b_{2}=24 \cdot 19\right.$ | $+0.264$ | +0.965 | 0 | 113 |
| $\left\{\begin{array}{l}b_{3}=23.88\end{array}\right.$ | 0 | 0 | $+1$ |  |

* The signs in parentheses refer to rotations of the phenyl groups in the anti-clockwise direction with respect to the $X$ axis in Figure 2.
amide $)+2 R\left(\mathrm{C}_{6} \mathrm{H}_{6}\right)-8 R(\mathrm{C}-\mathrm{H})$ is $1 \cdot 1$ c.c. smaller than the observed value, and this corresponds to a polarisability exaltation ( $\Delta b$ ) of $1.24 \AA^{3}$. In the calculations we assign an increment of polarisability ( $\Delta b / 2$ ) as operative along each phenyl 1,4 -axis. Conformations of NN -diphenylformamide are defined, in Table 6, by (equal) angles of rotation $\left(\alpha^{\circ}\right)$ of the phenyl groups, in the same sense from a theoretical planar model for which $\alpha=0^{\circ}$. The observed molar Kerr constant ( $406 \times 10^{-12}$ ) is in closest agreement with that calculated for $\alpha=52^{\circ}\left( \pm 5^{\circ}\right)$.

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19 A. I. Vogel, W. T. Cresswell, G. H. Jeffery, and J. Leicester, J., 1952, 514.


[^0]:    * Polarisability semi-axes of bonds $b_{\mathrm{L}}, b_{\mathrm{T}}$, or $b_{\mathrm{V}}$, or of molecules, $b_{1}, b_{2}$, or $b_{3}$, are quoted throughout in $10^{-24}$ c.c. $\left(\AA^{3}\right)$ units.
    ${ }^{16}$ R. J. Kurland and E. Bright Wilson, J. Chem. Phys., 1957, 27, 585.
    ${ }^{17}$ L. A. La Planche and M. T. Rogers, J. Amer. Chem. Soc., 1964, 86, 337.

[^1]:    * I.e., the semi-axes of acetamide less three $\mathrm{C}-\mathrm{H}$ bond contributions; the assumption here that $b_{2}=b_{3}$ for the $\mathrm{H}_{2} \mathrm{~N} \cdot \mathrm{CO} \cdot \mathrm{C}$ group should introduce no serious error in the estimates of ${ }_{\mathrm{m}} K$ calc. (for benzamide) in the presence of the highly anisotropic phenyl group.
    ${ }^{18}$ B. R. Penfold and J. C. B. White, Acta Cryst., 1959, 12, 130.

